AMDG

Name — Ms. Kresovic

Adv Geo — 9.9: Introduction to Trigonometry — Monday, March 24, 2014

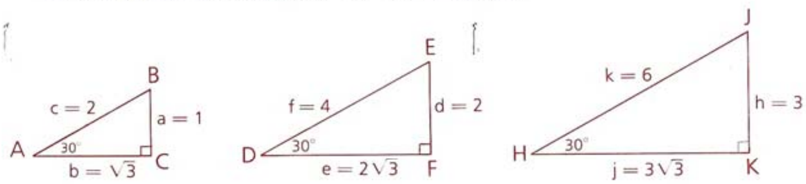
Objective

After studying this section, you will be able to

- Understand three basic trigonometric relationships

This section presents the three basic trigonometric ratios ***sine***, ***cosine***, and ***tangent***. The concept of similar triangles and the Pythagorean Theorem can be used to develop the ***trigonometry of right triangles.***

Consider the following 30°-60°-90° triangles.



Compare the length of the leg opposite the 30° angle with the length of the hypotenuse in each triangle.

In △ABC, $\frac{a}{c} = \frac{1}{2} = 0.5$. In △DEF, $\frac{d}{f} = \frac{2}{4} = 0.5$. In △HJK, $\frac{h}{k} = \frac{3}{6} = 0.5$.

If you think about similar triangles, you will see that in every 30°-60°-90° triangle,

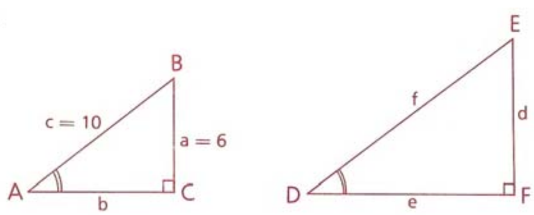
$$\frac{\text{leg opposite } 30^\circ \angle}{\text{hypotenuse}} = \frac{1}{2}$$

For each triangle shown, verify that $\frac{\text{leg adjacent to } 30^\circ \angle}{\text{hypotenuse}} = \frac{\sqrt{3}}{2}$.

For each triangle shown, find the ratio $\frac{\text{leg opposite } 30^\circ \angle}{\text{leg adjacent to } 30^\circ \angle}$.

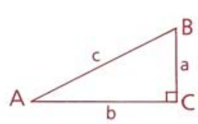
In △ABC and △DEF,

$\frac{a}{c} = \frac{d}{f} = \frac{6}{10} = \frac{3}{5}$



Engineers and scientists have found it convenient to formalize these relationships by naming the ratios of sides. You should memorize these three basic ratios.

Definition **Three Trigonometric Ratios**



$$\textit{sine} \text{ of } \angle A = \sin \angle A = \frac{\text{opposite leg}}{\text{hypotenuse}}$$

$$\textit{cosine} \text{ of } \angle A = \cos \angle A = \frac{\text{adjacent leg}}{\text{hypotenuse}}$$

$$\textit{tangent} \text{ of } \angle A = \tan \angle A = \frac{\text{opposite leg}}{\text{adjacent leg}}$$

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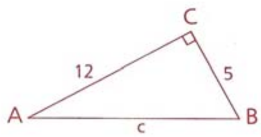
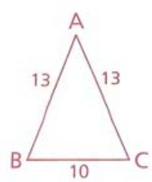
Class Examples

Problem 1 *Find:* **a** cos ∠A
b *tan* ∠B

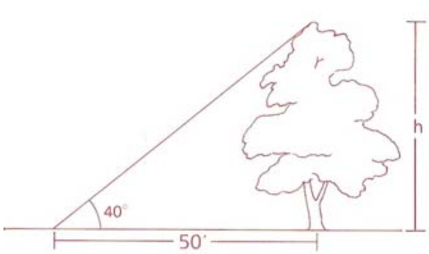


Problem 2 *Find the three trigonometric ratios for* ∠A *and* ∠B.

Problem 3 *△ABC is an isosceles triangle as marked. Find sin* ∠C.



Problem 4 *Use the fact that tan 40° ≈ 0.8391 to find the height of the tree to the nearest foot.*



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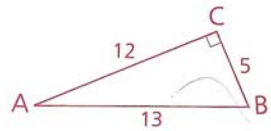
Homework

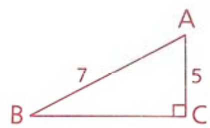
5 If $\tan \angle M = \frac{3}{4}$, find $\cos \angle M$. (Hint: Start by drawing the triangle.)

6 Using the figure as marked, name each missing angle.



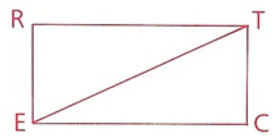
a $\frac{5}{12} = \tan \angle$ __?__ **b** $\frac{12}{13} = \cos \angle$ __?__ **c** $\frac{5}{13} = \sin \angle$ __?__

7 Find each quantity.



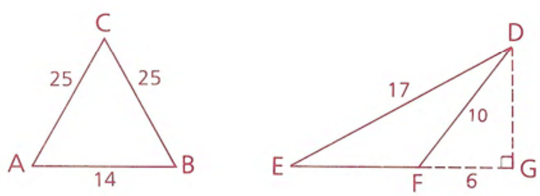
a BC **b** $\sin \angle A$ **c** $\tan \angle B$

8 Given: RECT is a rectangle.
ET = 26, RT = 24
Find: **a** $\sin \angle RET$ **b** $\cos \angle RET$

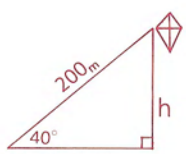


Problem Set B

9 Using the given figures, find
a $\cos \angle A$
b $\sin \angle E$
c $\sin \angle DFG$

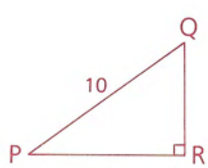


10 Use the fact that $\sin 40° \approx 0.6428$ to find the height of the kite to the nearest meter.

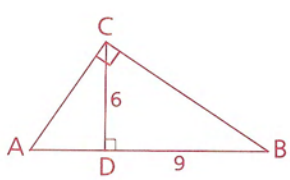


11 **a** If $\tan \angle A = 1$, find $m\angle A$.
b If $\sin \angle P = 0.5$, find $m\angle P$.

12 Given: $\sin \angle P = \frac{3}{5}$, PQ = 10
Find: $\cos \angle P$

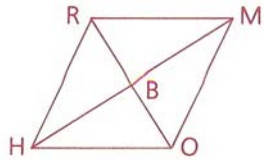


13 Using the figure, find
a $\tan \angle ACD$
b $\sin \angle A$



Problem Set B, *continued*

14 Given: RHOM is a rhombus.
RO = 18, HM = 24
Find: **a** cos ∠BRM **b** tan ∠BHO



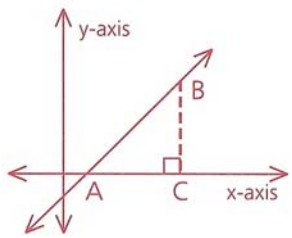
15 Given a trapezoid with sides 5, 10, 17, and 10, find the sine of one of the acute angles.

16 Given △ABC with ∠C = 90°, indicate whether each statement is true Always (A), Sometimes (S), or Never (N).

a sin ∠A = cos ∠B **b** sin ∠A = tan ∠A **c** sin ∠A = cos ∠

17 If △EQU is equilateral and △RAT is a right triangle with RA = 2, RT = 1, and ∠T = 90°, show that sin ∠E = cos ∠A.

18 If the slope of $\overleftrightarrow{AB}$ is $\frac{5}{8}$, find the tangent of ∠BAC.



Problem Set C

19 Use the definitions of the trigonometric ratios to verify the following relationships, given △ABC in which ∠C = 90°.

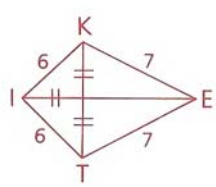
a $(\sin \angle A)^2 + (\cos \angle A)^2 = 1$

b $\dfrac{a}{\sin \angle A} = \dfrac{b}{\sin \angle B}$

c $\dfrac{\sin \angle A}{\cos \angle A} = \tan \angle A$

d $\sin \angle A = \cos (90° - \angle A)$

22 Given: KITE is a kite with sides as marked.
Find: tan ∠KEI



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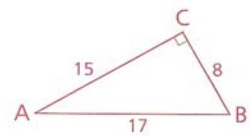
Classwork

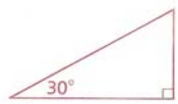
1 Find each ratio.

- **a** sin ∠A
- **b** cos ∠A
- **c** tan ∠A
- **d** sin ∠B
- **e** cos ∠B
- **f** tan ∠B



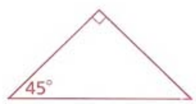
2 Find each ratio.

- **a** sin 30°
- **b** cos 30°
- **c** tan 30°
- **d** sin 60°
- **e** cos 60°
- **f** tan 60°



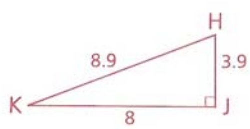
3 Find each ratio.

- **a** sin 45°
- **b** cos 45°
- **c** tan 45°



4 Find each ratio.

- **a** cos ∠H
- **b** tan ∠K



1a	
1b	
1c	
1d	
1e	
1f	
2a	
2b	
2c	
2d	
2e	
2f	
3a	
3b	
3c	
4a	
4b	