Name STU Dent Adv Geo 7

9.2: Introduction to Circles

Date W 26 feb 14

Ms. Kresovic

Objective

After studying this section, you will be able to

Begin solving problems involving circles

Example 1 Find the circumference and the area of \bigcirc O.



→

The circumference is found with the formula $C = \pi d$, where d is the diameter of the circle.

$$C = \pi d$$
 | dimension
= 14π + exact



The area is found with the formula $A = \pi r^2$, where r is the circle's radius.

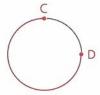
$$A = \pi r^2$$

$$= \pi (7^2)$$

$$= 49\pi$$
estimat

The circle's circumference is 14π , or about 43.98, inches and its area is 49π , or about 153.94, square inches.

An arc is made up of two points on a circle and all the points of the circle needed to connect those two points by a single path. The blue portion of the figure at the right is called arc CD (symbolized \widehat{CD}).



A

An <u>exact answer</u> is written in terms of pi (π) : 3π is exact.

An estimated value multiplies an estimate of pi: 9.42 is an estimated value of 3π .

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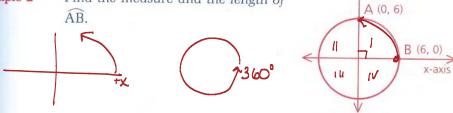
Date

y-axis

Adv Geo The measure of an arc is equivalent to the number of degrees it occupies. (A complete circle occupies 360°.) The length of an arc is a fraction of a circle's circumference, so it is expressed in linear units,

Example 2 Find the measure and the length of

such as feet, centimeters, or inches.



Since the arc is one fourth of the circle, its measure is $\frac{1}{4}(360)$, or 90. The arc's length (ℓ) can be expressed as a part of the circle's circumference.

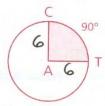
$$\ell = \frac{90}{360}C$$

$$= \frac{1}{4}\pi d$$

$$= \frac{1}{4}(\pi \cdot 12)$$

$$= 3\pi, \text{ or } \approx 9.42$$

A sector of a circle is a region bounded by two radii and an arc of the circle. The figure at the right shows sector CAT of OA.

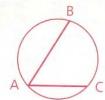


Since we know that CT has a measure of 90, we can calculate the area of sector CAT as a fraction of the area of OA.

Area of sector CAT =
$$\frac{90}{360}$$
(area of \odot A)
= $\frac{1}{4}(\pi \cdot 6^2)$
= 9π , or ≈ 28.27

A chord is a line segment joining two points on a circle. (A diameter is a chord that passes through the center of its circle.) An inscribed angle is an angle whose vertex is on a circle and whose sides are determined by two chords of the circle.

In the figure at the right, AB and AC are chords, and ∠BAC is an inscribed angle. ZBAC is said to intercept BC. (An intercepted arc is an arc whose endpoints are on the sides of an angle and whose other points all lie within the angle. Although ∠BAC intercepts only one arc, in Chapter 10 you will deal with some angles that intercept two arcs of a circle.)



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Problem 1

Find the circumference and the area

of ⊙P.

Solution

$$C = \pi d$$
 $A = \pi r^2$
 $= \pi (5.4)$ $= \pi (2.7^2)$
 $= 5.4\pi$, or ≈ 16.96 $= 7.29\pi$, or ≈ 22.90

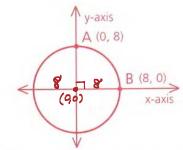


Problem 2

Given: Diagram as marked

Find: a mAB - deques

Some other unit ← b The length of \widehat{AB}



Solution

The circle's radius is 8, and \widehat{AB} is one fourth of the circle.

a
$$\widehat{\text{mAB}} = \frac{1}{4}(360)$$

= 90°

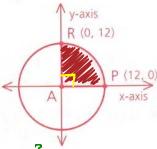
b Length of
$$\widehat{AB} = \frac{90}{360}C$$

$$= \frac{1}{4}(\pi \cdot 16)$$

$$= 4\pi, \text{ or } \approx 12.57$$
exact

Problem 3

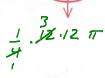
Find the area of the shaded region (sector PAR).



Solution

The radius of $\bigcirc A$ is 12, and $\widehat{mRP} = 90$.

Area of sector PAR =
$$\frac{90}{360}$$
 (area of \odot A)
= $\frac{1}{4}(\pi \cdot 12^2)$
= 36π , or ≈ 113.10



Problem 4

Harry Halph looked ahead to Chapter 10 and discovered that the measure of an inscribed angle is half the measure of its intercepted arc. Use this information to find the measure of inscribed angle DEF.

Solution

 \widehat{DF} is the arc intercepted by $\angle DEF$.

$$m \angle DEF = \frac{1}{2} (m\widehat{DF})$$
$$= \frac{1}{2} (80)$$
$$= 40$$

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Show that \triangle INS is a right triangle by

- a Finding m∠INS
- **b** Finding the slopes of \overrightarrow{IN} and \overrightarrow{NS}

lution

a \widehat{ICS} is one-half the circle, so $\widehat{mICS} = 180$. Since \widehat{ICS} is intercepted by inscribed angle INS,

$$m \angle INS = \frac{1}{2} (\widehat{mICS})$$
$$= \frac{1}{2} (180)$$
$$= 90$$

rise =

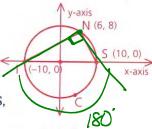
Therefore, \angle INS is a right angle, and \triangle INS is a right triangle.

b Recall that two lines are perpendicular if their slopes are opposite reciprocals.

Slope of
$$\overrightarrow{IN} = \frac{8-0}{6-(-10)} = \frac{1}{2}$$

Slope of
$$\overrightarrow{NS} = \frac{0-8}{10-6} = -2$$

Since $\overrightarrow{IN} \perp \overrightarrow{NS}$, $\triangle INS$ is a right triangle.



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Adv Geo **Homework**

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Date

C= 19.6 T ~ 61.58

Find the circumference and the area of $\bigcirc O$. $C = 19.6\pi$, or ≈ 61.58 ;

$$C = 19.6\pi$$
, or ≈ 61.58 ;
 $A = 96.04\pi$, or ≈ 301.72

2 Given: Diagram as marked

Find: a The measure of the arc from C to D (mCD) 90

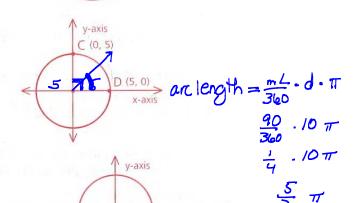
b The length of CD

$$\frac{40}{360}$$
 $10\pi = \frac{5}{2}$ $\pi = 2.5\pi$, or ≈ 7.85

3) Given: Diagram as marked

Find: a mEF 180

b The length of \widehat{EF} to the nearest tenth



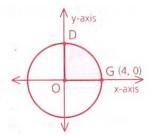
F (4, 0) x-axis

 $C = \pi d$

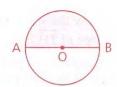
4 Given: Diagram as marked

Find: a The coordinates of D

b The area of the shaded region (sector DOG)

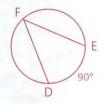


5 If AB = 10, what is the area of the shaded region (sector AOB)?



(-4, 0)

6 Find m∠F.



Name

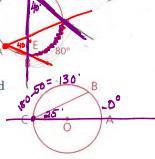
Date

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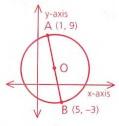
Adv Geo 7 Given: Diagram as marked

- Find: a m∠A 40
 - b m∠D 40

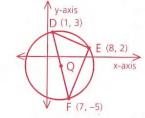
8 In \odot O, m $\widehat{AB} = 50$. Find m \widehat{BC} and m∠BCA.



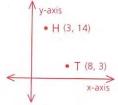
9 In the figure shown, \overline{AB} is a diameter. Find the coordinates of point O, the center of the circle.



10 Find the coordinates of Q, the center of the circle. Then use slopes to show that ΔDEF is a right triangle.



- 11 Copy the diagram, reflecting H across the y-axis to H'. Then find
 - a The coordinates of H'
 - b The slope of TH'



Problem Set B

- 12 In \bigcirc Q, m \widehat{HJ} = 20 and m \widehat{MK} = 40. The circumference of $\bigcirc Q$ is 27π .
 - a Find mJK.
 - b Find the length of JK.
 - c Find HM (the length of HM).

