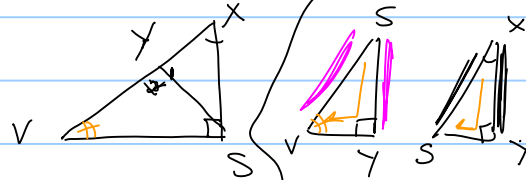


MAP:

7.  $G: \overline{SY}$  alt,  $\angle VSX \cong \angle L$

$P: XY \cdot SV = XS \cdot YS$



1.  $\overline{SY}$  alt,  $\angle VSX \cong \angle L$  1. Given

2.  $\triangle XYS \sim \triangle SYV$  2. Alt-Hyp  $\Rightarrow \sim \triangle$

3.  $XY/XS = YS/SV$  3.  $\sim \triangle \Rightarrow$  corr sds prop

4.  $XY \cdot SV = XS \cdot YS$  4. Means Extremes Product

$\triangle XYS \sim \triangle SYV?$

$$\frac{XY}{XS} = \frac{YS}{SV}$$

4c  $JO = 3\sqrt{2}$ ,  $JK = 3$ ,  $JM = ?$

leg<sup>2</sup> = (close)(whole)

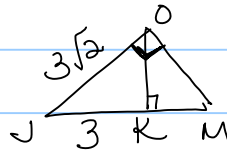
$$JO^2 = JK \cdot JM$$

$$(3\sqrt{2})^2 = 3 \cdot JM$$

$$9 \cdot 2 = 3 \cdot JM$$

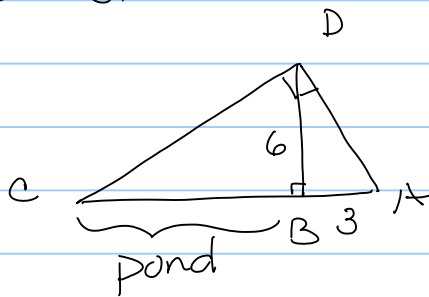
$$18/3 = JM$$

$$6 = JM$$



$P: \underline{XY} \cdot \underline{SV} = \underline{XS} \cdot \underline{YS}$

14.



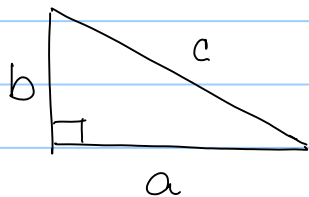
alt<sup>2</sup> = part · part

$$DB^2 = CB \cdot BA$$

$$6^2 = \text{pond} \cdot 3$$

$$12\text{m} = \text{pond}$$

### 9.4: Geometry's Most ELEGANT THEOREM

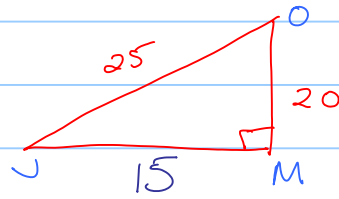
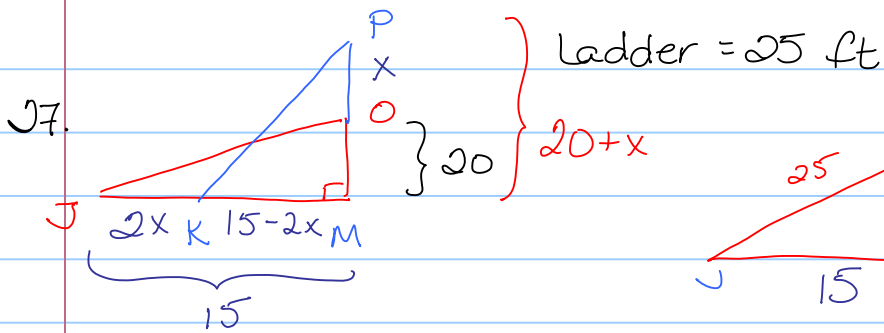


$$c^2 = a^2 + b^2$$

$$\text{hyp}^2 = \text{leg}^2 + \text{leg}^2$$

T69: rt  $\Delta \Rightarrow a^2 + b^2 = c^2$

T70:  $a^2 + b^2 = c^2 \Rightarrow \text{rt} \Delta$

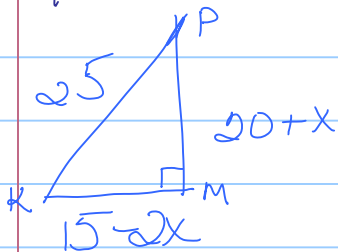


(leg, leg, hyp)

Reduced  
△ Principle

$$\begin{aligned} & (15, 20, 25) \\ 5 & \left( \frac{3}{4}, 5 \right) \\ & a^2 + 4^2 = 5^2 \\ & a^2 = 25 - 16 \\ & a^2 = 9 \\ & a = 3 \end{aligned}$$

G: JK = 2(PO)



$$\begin{aligned} \text{leg}^2 + \text{leg}^2 &= \text{hyp}^2 \\ (20+x)^2 + (15-2x)^2 &= 25^2 \\ \underbrace{(20+x)(20+x)} + \underbrace{(15-2x)(15-2x)} &= 625 \end{aligned}$$

$$\underline{\underline{400}} + \underline{\underline{20x}} + \underline{\underline{20x}} + \underline{\underline{x^2}} + \underline{\underline{225}} - \underline{\underline{30x}} - \underline{\underline{30x}} + \underline{\underline{4x^2}} = 625$$

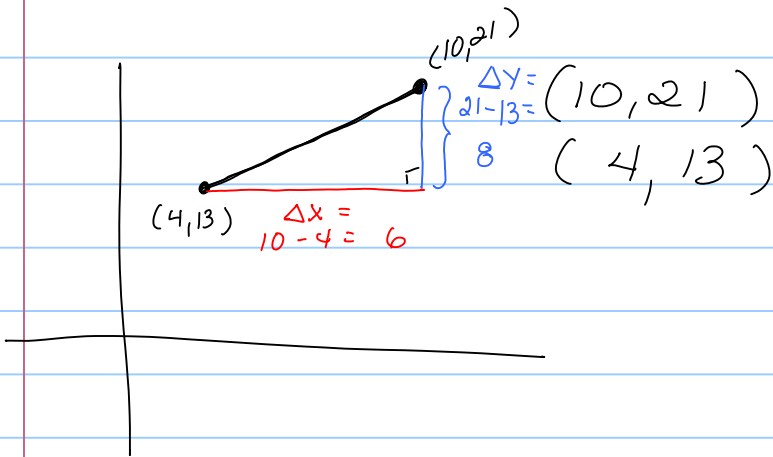
$$5x^2 - 20x + 625 = 625$$

$$5x^2 - 20x = 0$$

$$5x(x - 4) = 0$$

$$x = 0 \text{ or } 4$$

# 9.5: Distance Formula



$$(6, 8, 10)$$

$$2(3, 4, 5)$$

$$3^2 + 4^2 = c^2$$

$$9 + 16 = c^2$$

$$25 = c^2$$

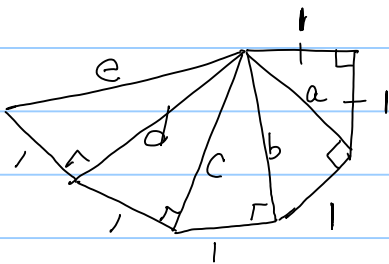
$$5 = c$$

Pyth. Triples: rt Δ sides integers  
(3, 4, 5)

$$\sqrt{\text{leg}^2 + \text{leg}^2} = \text{Dist}$$

$$\sqrt{\Delta x^2 + \Delta y^2}$$

$$\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$



$$1^2 + 1^2 = a^2$$

$$2 = a^2$$

$$\sqrt{2} = a$$

$$\sqrt{2^2 + 1^2} = b^2$$

$$2 + 1 = b^2$$

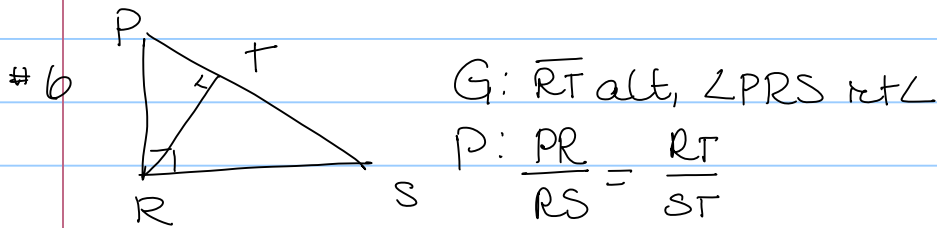
$$3 = b^2$$

$$\sqrt{3} = b$$

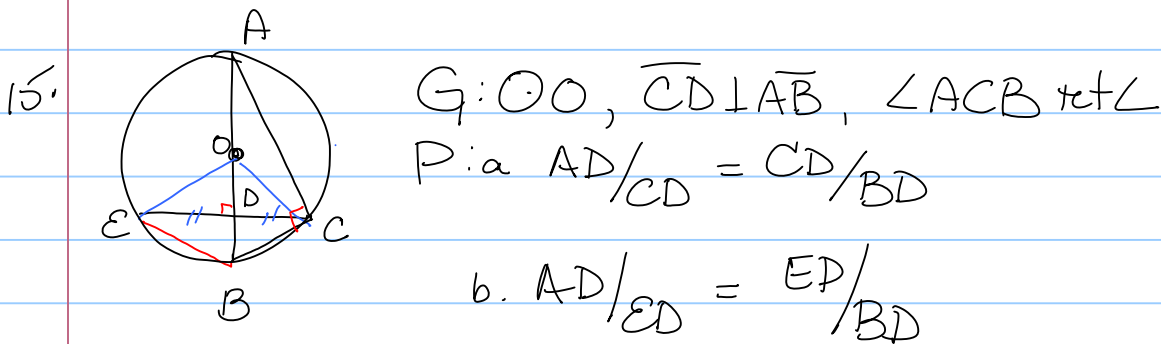
find  $e = \sqrt{6}$

P8

see 9.3:7 above

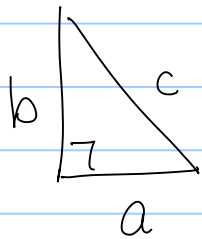


1.  $\overline{RT}$  alt,  $\angle PRS$  rt  $\angle$       1. Given
2.  $\triangle PRS \sim \triangle RTS$       2. Alt Hyp  $\Rightarrow \sim \triangle$
3.  $\frac{PR}{RS} = \frac{RT}{ST}$       3.  $\sim \triangle \Rightarrow$  corr sds prop



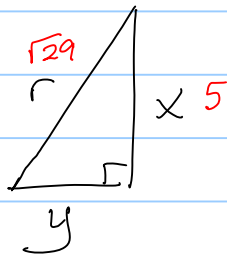
1.  $\odot O$ ,  $\overline{CD} \perp \overline{AB}$ ,  $\angle ACB$  rt  $\angle$       1. Given
2.  $\triangle ADC \sim \triangle CDB$       2. alt-Hyp  $\Rightarrow \sim \triangle$
3.  $\frac{AD}{DC} = \frac{CD}{DB}$       3.  $\sim \triangle \Rightarrow$  corr sds prop
4. Draw  $\overline{OE}$  &  $\overline{OC}$       4. Aux
5.  $\overline{OE} \cong \overline{OC}$       5.  $\odot \Rightarrow \cong$  rad
6.  $\angle ODE$  &  $\angle ODC$  rt  $\angle$ s      6.  $\perp \Rightarrow$  rt  $\angle$ s
7.  $\overline{OD} \cong \overline{OD}$       7. Ref
8.  $\triangle ODE \cong \triangle ODC$       8. HL (6, 5, 7)
9.  $\overline{ED} \cong \overline{DC}$       9. CPCTC
10.  $\frac{AD}{ED} = \frac{ED}{DB}$       10. Substitute

# 9.4: Geometry's most elegant theorem



T69: rt  $\Delta \Rightarrow c^2 = a^2 + b^2$   
 T70:  $a^2 + b^2 = c^2 \Rightarrow$  rt  $\Delta$

Ex: If:  $x=5, r=\sqrt{29}$



$$x^2 + y^2 = r^2$$

$$5^2 + y^2 = (\sqrt{29})^2$$

$$25 + y^2 = 29$$

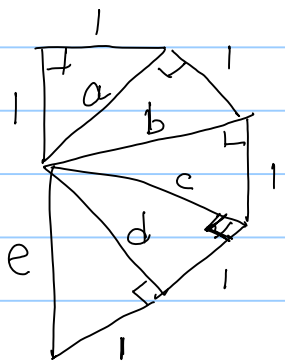
$$y^2 = 29 - 25$$

$$y^2 = 4$$

$$y = 2$$

(Q: Why not neg 2?)

A: Can't have neg length!



$$\text{leg}^2 + \text{leg}^2 = \text{hyp}^2$$

$$1^2 + 1^2 = a^2$$

$$1 + 1 = a^2$$

$$2 = a^2$$

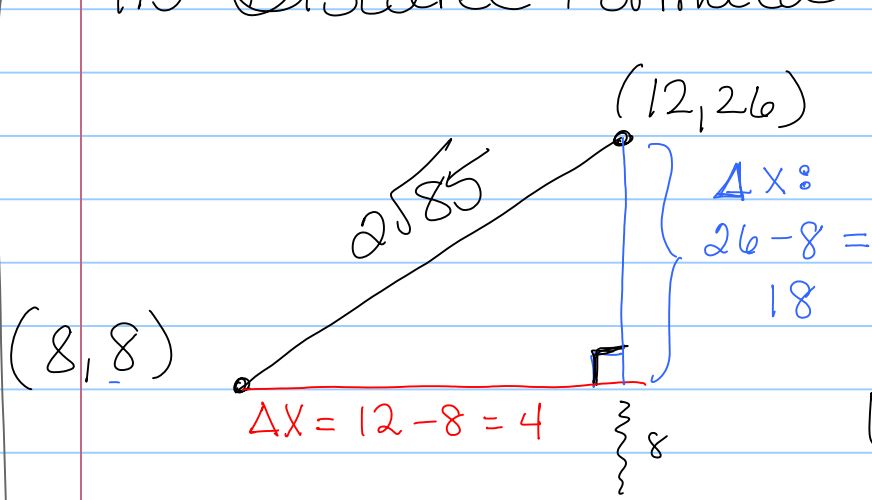
$$\sqrt{2} = a$$

$$1^2 + (\sqrt{2})^2 = b^2$$

$$\sqrt{3} = b$$

find  $e = \sqrt{4}$

# 9.5: Distance Formula



$$\begin{pmatrix} 12, 26 \\ 8, 8 \end{pmatrix}$$

$$\begin{aligned} \text{leg}^2 + \text{leg}^2 &= \text{hyp}^2 \\ (4, 18, 2\sqrt{85}) \end{aligned}$$

Reduced  $\Delta$  principle:  $2(2, 9, \sqrt{85})$

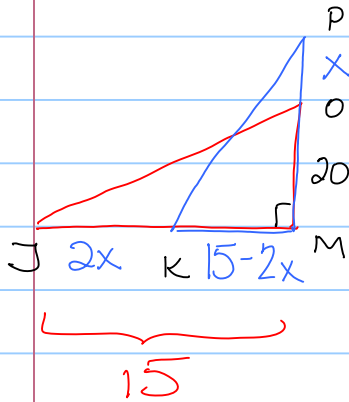
$$2^2 + 9^2 = ?$$

$$85 = \text{hyp}^2$$

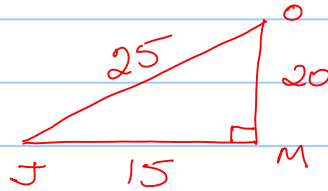
$$\sqrt{85} = \text{hyp}$$

p390

9.4:27



Ladder = 25 ft = JP



$$(JM, 20, 25)$$

$$5 \left( \frac{4}{5}, \frac{3}{5}, 1 \right)$$

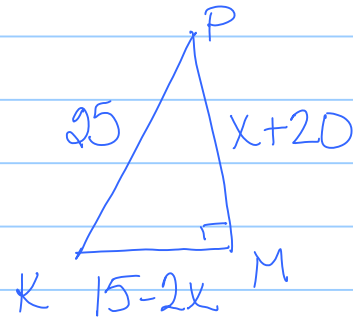
$$?^2 + 16 = 25$$

$$? = 3$$

$$JM = 3(5) = 15$$

Pyth Triples  
(3, 4, 5)

$$4(3, 4, 5) = 12, 16, 20$$



$$PM^2 + KM^2 = PK^2$$

$$(x+20)^2 + (15-2x)^2 = 25^2$$

$$(x+20)(x+20) + (15-2x)(15-2x) = 625$$

$$\underline{x^2} + \underline{20x} + \underline{20x} + \underline{400} + \underline{225} - \underline{30x} - \underline{30x} + \underline{4x^2} = 625$$

$$5x^2 - 20x + 625 = 625$$

$$5x^2 - 20x = 0$$

$$5x(x-4) = 0$$

Then  $x = 0$  or  $4$ .

Find KM:  $15 - 2x$

$$KM = \frac{15}{7} \text{ or } \boxed{7 \text{ ft}}$$