

$$1d \ (1, 1\frac{1}{3}, _) \rightarrow (\frac{3}{3}, \frac{4}{3}, _) \rightarrow \frac{1}{3} (3, 4, 5) \rightarrow \frac{5}{3}$$

$$5b \ (6, \overset{\text{hyp}}{\downarrow} 8) \rightarrow 2(3, \sqrt{7}, 4) \rightarrow \boxed{2\sqrt{7}}$$

$leg^2 + leg^2 = hyp^2$
 $16 - 9 = 7$

$$f \ (15, _, 20) \rightarrow 5(3, \sqrt{7}, 4) \rightarrow \underline{5\sqrt{7}}$$

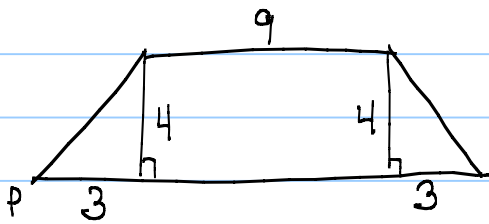
$$5d \ (_, 12, 13) \rightarrow .1(5, 12, 13) \rightarrow .5$$

$leg^2 + leg^2 = hyp^2$

$$5i \ (5\sqrt{7}, _, 13\sqrt{7}) \rightarrow \sqrt{7}(5, 12, 13) \rightarrow \boxed{12\sqrt{7}}$$

$$4d \ (_, 1\frac{1}{2}, 1\frac{7}{10}) \rightarrow (_, \frac{15}{10}, \frac{17}{10}) \rightarrow \frac{1}{10}(8, 15, 17) \rightarrow \frac{8}{10} \text{ or } \frac{4}{5}$$

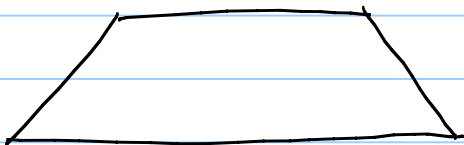
17



$$2\Delta s + \text{Rect}$$

$$2(\frac{1}{2})3 \cdot 4 + 4 \cdot 9$$

$$12 + 36 = 48$$



$$9.a(8\sqrt{5}, 16, _) \rightarrow 8(\sqrt{5}, 2, 3) \rightarrow 24$$

$$5+4=9 \quad 9+9=3$$

$$9.b(200__700) \rightarrow 100 \quad 2, \sqrt{5}, 7 \rightarrow 300\sqrt{5}$$

$$4+x^2=49$$

$$x^2=45$$

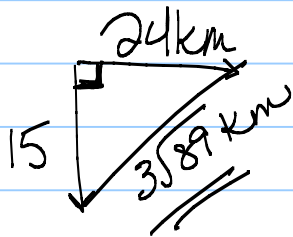
$$x=\sqrt{9}\sqrt{5}$$

12 diag rhomb bis each other & \perp

$$\text{diag } 48 \& 14 \rightarrow 24 \& 7$$

$$24 \quad \begin{array}{c} \text{side 2} \\ 25 \\ 7 \end{array} \Rightarrow P=100$$

13.



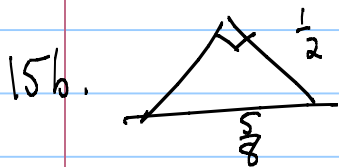
$$L: \frac{16 \text{ km}}{\text{hr}} \cdot \frac{3 \text{ hrs}}{2} = 24 \text{ km}$$

$$M: \frac{5 \text{ km}}{\text{hr}} \cdot \frac{3 \text{ hr}}{2} = 15 \text{ km}$$

$$(15, 24, _)$$

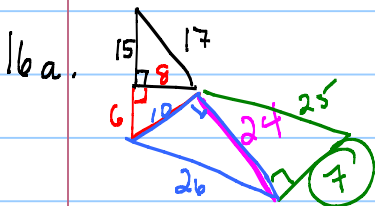
$$3(5, 8, \sqrt{89})$$

$$25+64=89$$



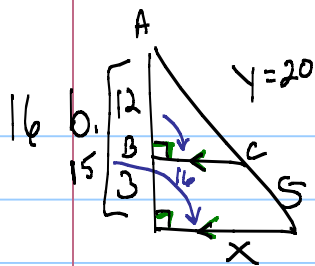
$$\left(\frac{1}{2} - \frac{5}{8}\right) \rightarrow \left(\frac{4}{8} - \frac{5}{8}\right) \Rightarrow \frac{1}{8} \left(4 - \overset{\text{hyp}}{5}\right) \rightarrow \left(\frac{3}{8}\right)$$

$$25-16=9$$



$$(10, 24, 26)$$

$$2(5, 12, 13)$$

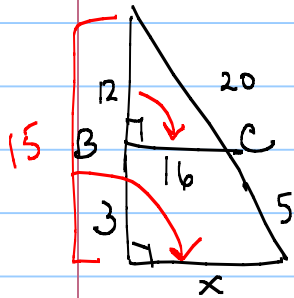


$$y \rightarrow \text{side splitter} \rightarrow \frac{12}{3} = \frac{y}{5} \quad y = 20$$

$$x \rightarrow \sim \triangle \rightarrow$$

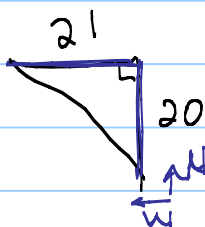
$$BC \Rightarrow (12 - 20) \rightarrow 4(3 \underline{4} 5) \rightarrow \underline{16} \text{ then } \frac{12}{16} = \frac{15}{x}$$

$$\frac{3}{4} = \frac{15}{x} \rightarrow x = 20$$



(18)

$$\frac{w}{n} = \frac{w}{n}$$

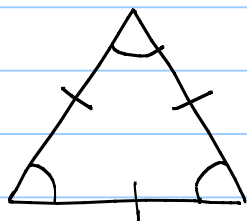


$$20^2 + 21^2 =$$

$$400 + 441 = 841$$

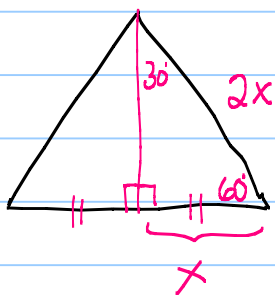
$$\sqrt{841} = 29 \text{ km}$$

9.7 Special Rt \triangle s



Equilat \rightarrow Equi \angle

What's the measure of an \angle in an equilateral triangle? 60° !



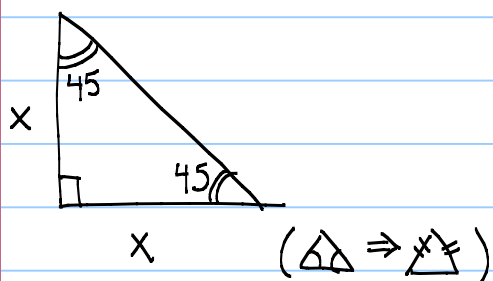
$$x^2 + ?^2 = (2x)^2$$

$$?^2 = 4x^2 - x^2$$

$$? = \sqrt{3x^2} = \sqrt{3} \sqrt{x^2} = x\sqrt{3}$$

In any
sides are

30°	60°	90°
x	$x\sqrt{3}$	$2x$



then by Pyth Thm

$$\text{leg}^2 + \text{leg}^2 = \text{hyp}^2$$

$$x^2 + x^2 = \text{hyp}^2$$

$$2x^2 = \text{hyp}^2$$

$$\sqrt{2x^2} = \text{hyp}$$

$$x\sqrt{2} = \text{hyp}$$

In any $45^\circ 45^\circ 90^\circ$
 $x \quad x \quad x\sqrt{2}$

PopQuizzes coming up :

1 question

Q: What are the 6 common families of rt \triangle s?

A: 1. (3, 4, 5)

2. (5, 12, 13)

3. (7, 24, 25)

4. (8, 15, 17)

5. (30, 60, 90) $\Leftrightarrow (x, x\sqrt{3}, 2x)$

6. (45, 45, 90) $\Leftrightarrow (x, x, x\sqrt{2})$

9.7

1a.	30	60	90
	x	$x\sqrt{3}$	2x
	<u>7</u>	<u>$7\sqrt{3}$</u>	14

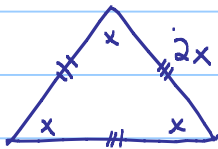
$$\text{if } 2x = 14$$

$$x = 7$$

1b.	30	60	90
	x	$x\sqrt{3}$	2x
	10	<u>$10\sqrt{3}$</u>	<u>20</u>

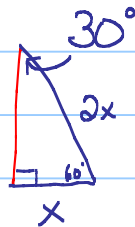
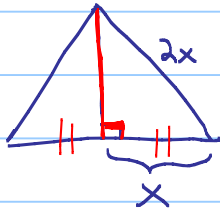
4a	45	45	90
	x	x	$x\sqrt{2}$
	8		<u>$8\sqrt{2}$</u>

P7 9.7 Special Rt \triangle s



$$3x = 180$$

$$x = 60$$



30	60	90
x	$x\sqrt{3}$	$2x$

$$2x = 20$$

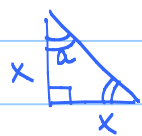
$$x = 10$$

$$\text{leg}^2 + \text{leg}^2 = \text{hyp}^2$$

$$x^2 + ?^2 = (2x)^2$$

$$?^2 = 4x^2 - x^2 = 3x^2$$

$$? = \sqrt{3} \sqrt{x^2} = x\sqrt{3}$$



$$a = 45^\circ$$

$$\text{leg}^2 + \text{leg}^2 = \text{hyp}^2$$

$$x^2 + x^2 = \text{hyp}^2$$

$$2x^2 = \text{hyp}^2$$

$$\sqrt{2} \cdot \sqrt{x^2} = \text{hyp}$$

$$x\sqrt{2} = \text{hyp}$$

45	45	90
x	x	$x\sqrt{2}$

Q: If hyp = 20
what's side opp 45° ?

$$\frac{x\sqrt{2}}{\sqrt{2}} = \frac{20}{\sqrt{2}}$$

$$x = \frac{20}{\sqrt{2}} \cdot \frac{\sqrt{2}}{\sqrt{2}} = \frac{20\sqrt{2}}{2} = 10\sqrt{2}$$

P7+8

Future Pop Quizzer!

Q: What are the 6 common Families of Rt \triangle s?

A: 1. (3, 4, 5)

2. (5, 12, 13)

3. (7, 24, 25)

4. (8, 15, 17)

5. $(30^\circ, 60^\circ, 90^\circ) \Leftrightarrow (x, x\sqrt{3}, 2x)$

6. $(45^\circ, 45^\circ, 90^\circ) \Leftrightarrow (x, x, x\sqrt{2})$

} backbone of
trigonometry

9.7: 405/ 1-10, 12,

Chapter review, p 429, 1-16

1a	30	60	90	1b	30	60	90
	x	$x\sqrt{3}$	$2x$		x	$x\sqrt{3}$	$2x$
	<u>7</u>	<u>$7\sqrt{3}$</u>	14		10	<u>$10\sqrt{3}$</u>	<u>20</u>

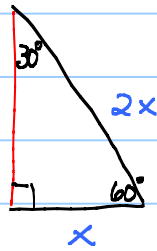
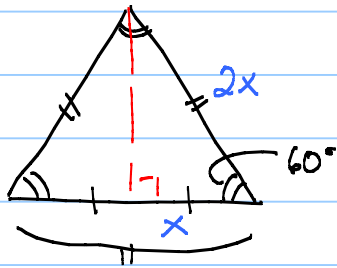
1c	30	60	90	1d	30	60	90
	x	$x\sqrt{3}$	$2x$		x	$x\sqrt{3}$	$2x$

1e	30	60	90
	x	$x\sqrt{3}$	$2x$

2a	30	60	90
	x	$x\sqrt{3}$	$2x$
	<u>$2\sqrt{3}$</u>	6	<u>$4\sqrt{3}$</u>

IF $\frac{x\sqrt{3}}{\sqrt{3}} = \frac{6}{\sqrt{3}}$, THEN $x = \frac{6}{\sqrt{3}} \frac{\sqrt{3}}{\sqrt{3}}$, $x = 2\sqrt{3}$

9.7: Special Families of Rt \triangle



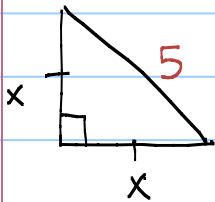
30	60	90
x	$x\sqrt{3}$	2x

$$\text{leg}^2 + \text{leg}^2 = \text{hyp}^2$$

$$x^2 + ?^2 = (2x)^2$$

$$?^2 = 4x^2 - x^2 \text{ or } 3x^2$$

$$? = \sqrt{3} \sqrt{x^2} \text{ or } x\sqrt{3}$$



45	45	90
x	x	$x\sqrt{2}$
$\frac{5\sqrt{2}}{2}$	$\frac{5\sqrt{2}}{2}$	5

$$\text{then } x\sqrt{2} = 5 \frac{\sqrt{2}}{\sqrt{2} \sqrt{2}}$$

$$x = \frac{5}{2} \sqrt{2}$$

$$\text{leg}^2 + \text{leg}^2 = \text{hyp}^2$$

$$x^2 + x^2 = h^2$$

$$2x^2 = h^2$$

$$\sqrt{2x^2} = h$$

$$x\sqrt{2} = h$$

9,7

1 a

30	60	90	
x	$x\sqrt{3}$	$2x$	$2x=14$
<u>7</u>	<u>$7\sqrt{3}$</u>	14	

b.

30	60	90
x	$x\sqrt{3}$	$2x$
10	<u>$10\sqrt{3}$</u>	<u>20</u>

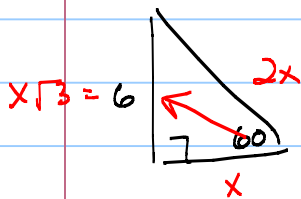
c

d

e

2a.

30	60	90	
x	$x\sqrt{3}$	$2x$	then $6 = x\sqrt{3}$
<u>$2\sqrt{3}$</u>	6	<u>$4\sqrt{3}$</u>	$x = \frac{6}{\sqrt{3}} \frac{\sqrt{3}}{\sqrt{3}}$ or $\frac{6}{3} \sqrt{3}$ or $2\sqrt{3}$



9.7: 405/ 1-10, 12,

Chapter review, p 429, 1-16