

NAME

Ms. Kresovic

Adv Geo –

Wednesday 6 March 2013

9.5: The Distance Formula

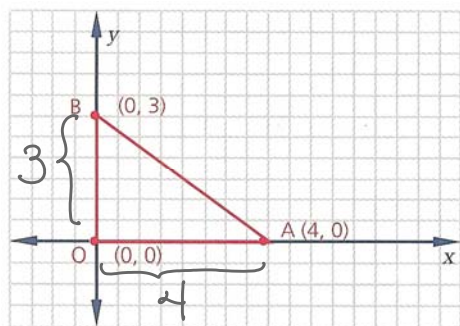
Objective

After studying this section, you will be able to

- Use the distance formula to compute lengths of segments in the coordinate plane

Prior Knowledge:

Pythagorean Theorem



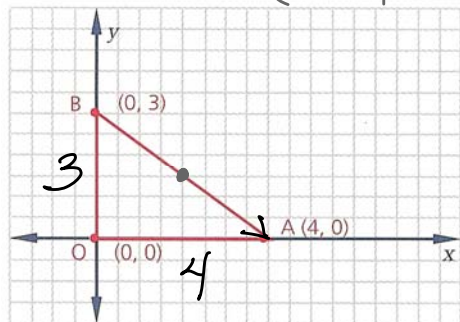
$$\begin{aligned} \textcircled{I} \quad 3^2 + 4^2 &= AB^2 \\ 9 + 16 &= AB^2 \\ 25 &= AB^2 \\ 5 &= AB \end{aligned}$$

↑

$$\begin{aligned} \textcircled{II} \quad &\sqrt{\Delta y^2 + \Delta x^2} \\ &\sqrt{(3-0)^2 + (4-0)^2} \\ &\sqrt{9 + 16} \\ &\sqrt{25} \\ &5 = AB \end{aligned}$$

↑

Midpoint formula \rightarrow (AVE X's, AVE Y's)



$$\left(\frac{0+4}{2}, \frac{3+0}{2} \right) = \left(2, \frac{3}{2} \right)$$

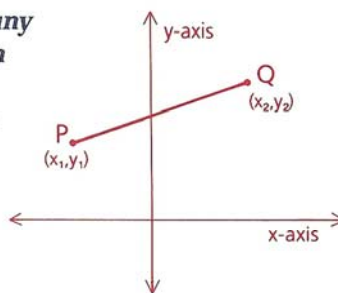
$$\text{Slope: } \frac{\Delta y}{\Delta x} = \frac{3-0}{0-4} = \boxed{\frac{3}{-4}}$$

Theorem 71

If $P = (x_1, y_1)$ and $Q = (x_2, y_2)$ are any two points, then the distance between them can be found with the formula

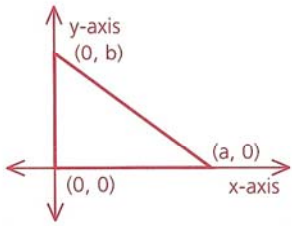
$$PQ = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2} \text{ or}$$

$$PQ = \sqrt{(\Delta x)^2 + (\Delta y)^2}$$

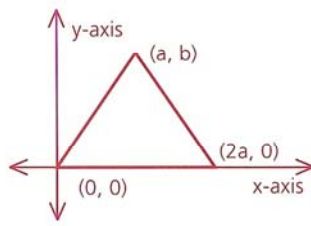


When doing coordinate proofs (sometimes called analytic proofs), you may select any convenient position in the coordinate plane for the figure as long as *complete generality is preserved*. Here are some convenient locations for a right triangle, an isosceles triangle, and a parallelogram.

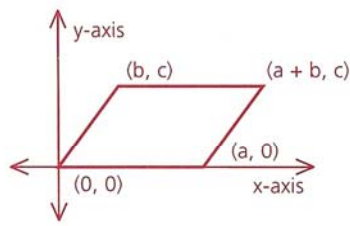
Right Triangle



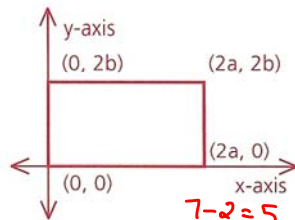
Isosceles Triangle



Parallelogram

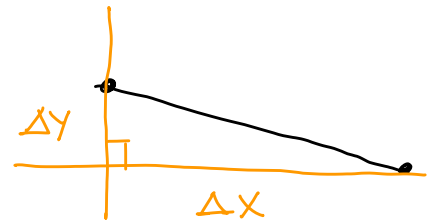
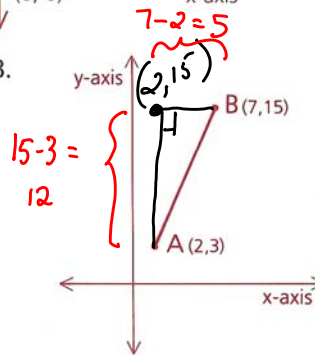


When midpoints are involved in a problem, it is helpful to use coordinates that make computations easier. For example, you could locate a rectangle as shown at the right.



Problem 1 If $A = (2, 3)$ and $B = (7, 15)$, find AB .

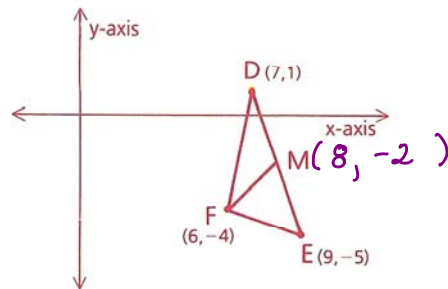
$$\begin{aligned} &\sqrt{(7-2)^2 + (15-3)^2} \\ &\sqrt{5^2 + 12^2} \\ &\sqrt{25 + 144} \\ &\sqrt{169} \\ &13 \end{aligned}$$



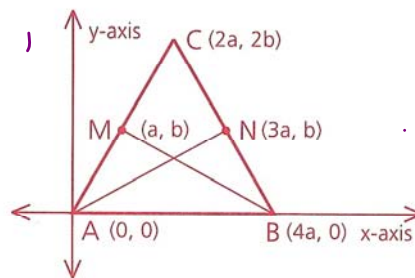
Problem 2 If $D = (7, 1)$, $E = (9, -5)$, and $F = (6, -4)$, find the length of the median from F to \overline{DE} .

$$\begin{aligned} FM &= \sqrt{(8-6)^2 + (-2-(-4))^2} \\ &= \sqrt{4 + 4} \\ &= \sqrt{8} \\ FM &= 2\sqrt{2} \end{aligned}$$

↳ mdpt



Problem 3 Prove: The medians to the legs of an isosceles triangle are congruent.



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1 Find the distance between each pair of points.

$$\begin{array}{l} \text{a } \sqrt{(4-6)^2 + (0-0)^2} \\ \sqrt{(-2)^2 + 0^2} \\ \sqrt{4} \\ 2 \end{array}$$

a (4, 0) and (6, 0)

b (2, 3) and (2, -1)

c (4, 1) and (7, 5)

d (-2, -4) and (-8, 4)

e The origin and (2, 5)

f (2, 1) and (6, 3)

2 Find the perimeter of $\triangle ABC$ if $A = (2, 6)$, $B = (5, 10)$, and $C = (0, 13)$.

3 Show that the triangle with vertices at (8, 4), (3, 5), and (4, 10) is a right triangle by using



a The distance formula

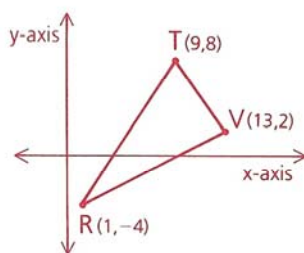
b Slopes

- 4 Use the distance formula to show that $\triangle DOG$ is equilateral if $D = (6, 0)$, $O = (0, 0)$, and $G = (3, 3\sqrt{3})$.

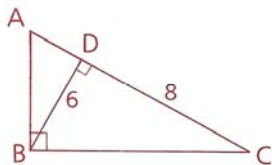
- 5 Find the area of the circle that passes through $(9, -4)$ and whose center is $(-3, 5)$.

- 6 Given: $\triangle RTV$ as shown

- Find: **a** The length of the median from T
b The length of the segment joining the midpoints of \overline{RT} and \overline{TV}

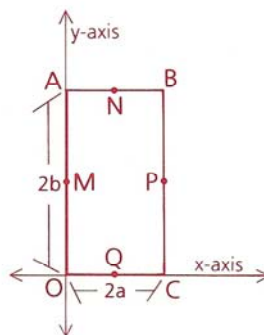


- 7 Find AD and BC .



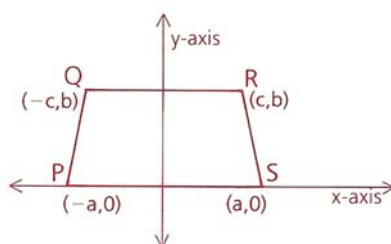
8 Given: Rectangle ABCO

- Find the coordinates of A, B, C, and O.
- Find the coordinates of M, N, P, and Q, the midpoints of the sides.
- Find the slopes of \overline{MN} , \overline{QP} , \overline{MQ} , and \overline{NP} . What can we conclude about MNPQ?
- Find the lengths of \overline{MN} , \overline{QP} , \overline{MQ} , and \overline{NP} . What can we now conclude about MNPQ?



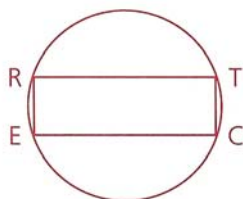
9 Given: Trapezoid PQRS

- Find PQ and SR and verify that PQRS is an isosceles trapezoid.
- Prove that the diagonals \overline{PR} and \overline{QS} are congruent.



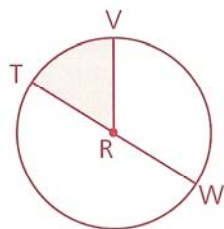
11 In rectangle RECT, $RE = 5$ and $EC = 12$.

- Find the circumference of the circle.
- Find the area of the circle to the nearest tenth.



- 13 Given: $\odot R$, $m\widehat{VW} = 120$,
 $RW = 9$

Find: **a** The area of sector TRV to the nearest tenth
b The difference, to the nearest tenth, between the length of \overline{TW} and the length of \widehat{VW}



- 15 Find, to the nearest tenth, the perimeter of a quadrilateral with vertices $A = (2, 1)$, $B = (7, 3)$, $C = (12, 1)$, and $D = (7, -4)$, and give the figure's most descriptive name.

- 20 The point $(5, y)$ is equidistant from $(1, 4)$ and $(10, -3)$. Find y .

- 22 A model rocket shot up to a point 20 m above the ground, hitting a smokestack, and then dropped straight down to a point 11 m from its launch site. Find, to the nearest meter, the total distance traveled from launch to touchdown.

